

# **SQUARE NUMBERS**

# Picture Puzzles

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Publisher ... Mathematics Centre  
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This Picture Puzzle is based on  
... Task 111, *Square Numbers*  
Teaching Notes  
... [mathematicscentre.com/picturepuzzles/teachingnotes](http://mathematicscentre.com/picturepuzzles/teachingnotes)

# Picture Puzzles

## To Do

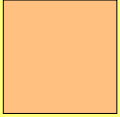
1. Look at visual patterns to find numbers.
2. Check your answers by calculating in two ways.
3. Learn more about Square Numbers.

## You Need

- Square tiles or cube blocks
- Square graph paper

# Picture Puzzles

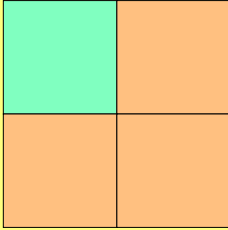
Make this...



$$S_1 = 1$$

# Picture Puzzles

Now this...

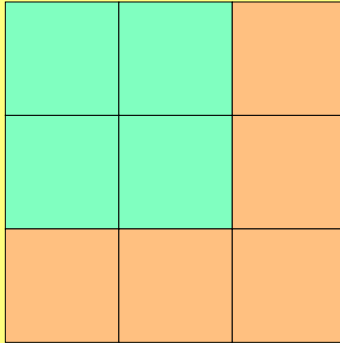


$$S_1 = 1$$

$$S_2 = 4$$

# Picture Puzzles

Now this...



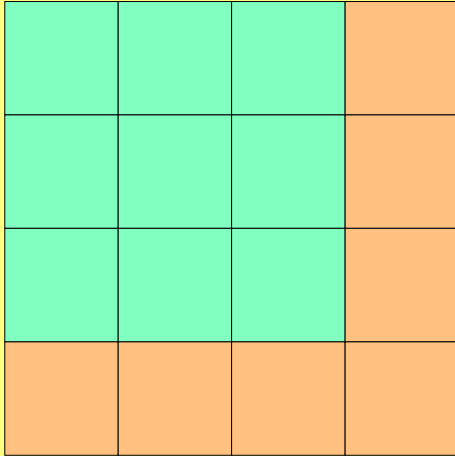
$$S_1 = 1$$

$$S_2 = 4$$

$$S_3 = 9$$

# Picture Puzzles

Now this...



$$S_1 = 1$$

$$S_2 = 4$$

$$S_3 = 9$$

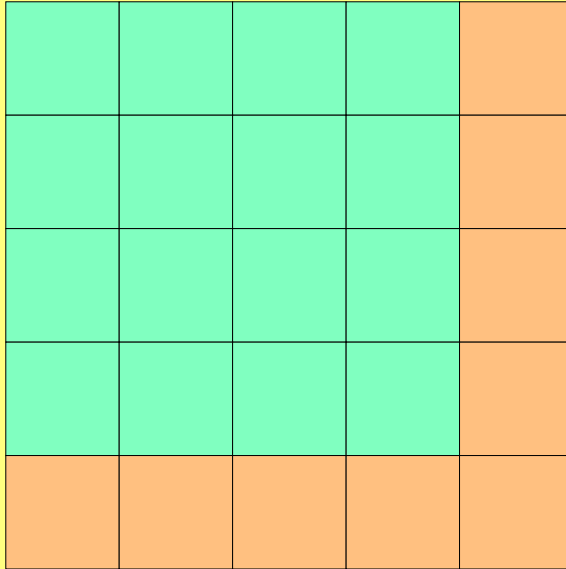
$$S_4 = 16$$

**Predict  $S_5$**



**Predict  $S_5$  another way.**

# Picture Puzzles



$$S_1 = 1$$

$$S_2 = 4$$

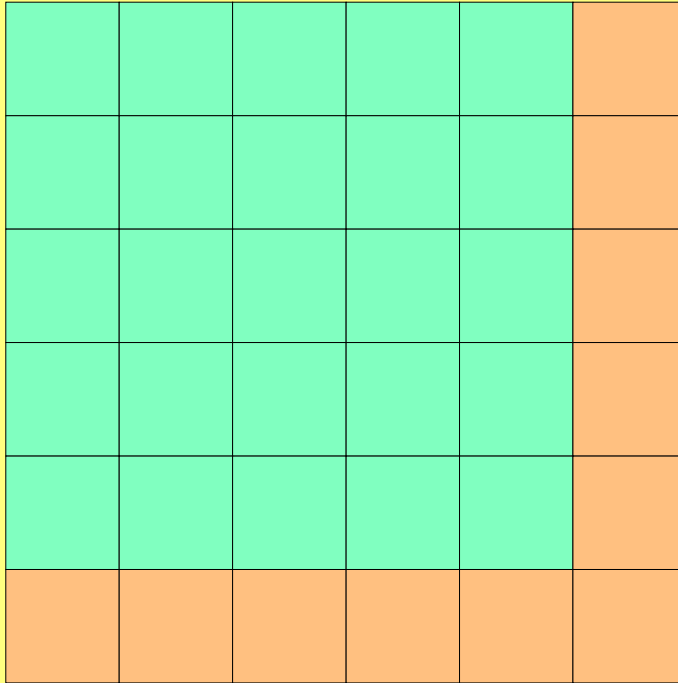
$$S_3 = 9$$

$$S_4 = 16$$

$$S_5 = 25$$

**Predict  $S_6$  in two different ways.**

# Picture Puzzles



$$S_1 = 1$$

$$S_2 = 4$$

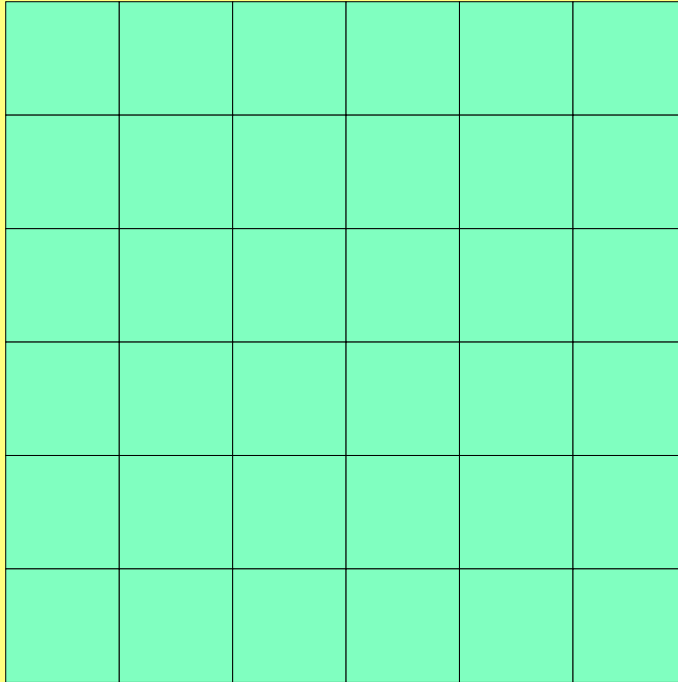
$$S_3 = 9$$

$$S_4 = 16$$

$$S_5 = 25$$

$$S_6 = 36$$

# Picture Puzzles



$$S_1 = 1$$

$$S_2 = 4$$

$$S_3 = 9$$

$$S_4 = 16$$

$$S_5 = 25$$

$$S_6 = 36$$

...

$$S_{20} = ??$$

**You might be correct for  $S_{20}$**

**Can you check it another way?**

**Choose any size square.  
Calculate the number of small  
squares in two different ways.**

**Write and draw about  
Square Numbers  
in your journal.**



**Can you explain why the L-shape  
must be an odd number?**

**Picture  
Puzzles**

**more**

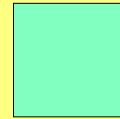
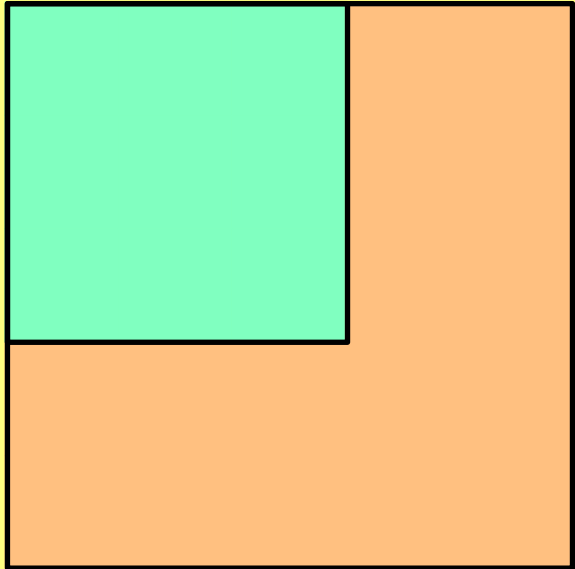
**Picture  
Puzzles**

# Picture Puzzles

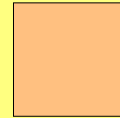
## To Do

1. Place one square on top of another square.
2. Calculate the uncovered area - difference between the two squares.
3. Check your answer by calculating in two ways.

# Picture Puzzles

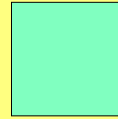
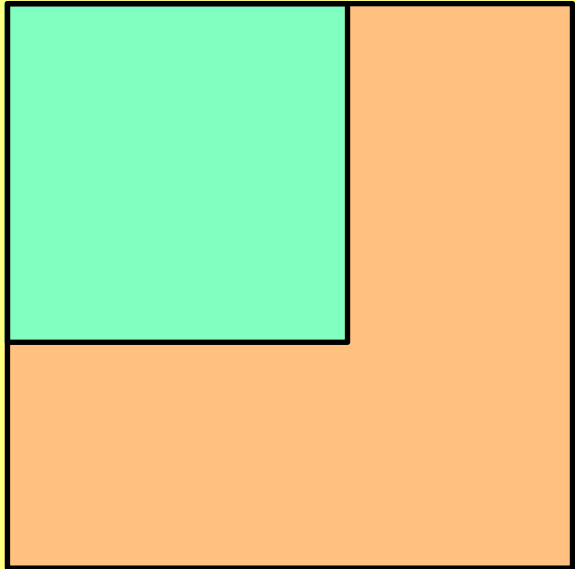


$S_3$  on top

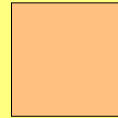


$S_5$  below

# Picture Puzzles



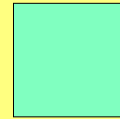
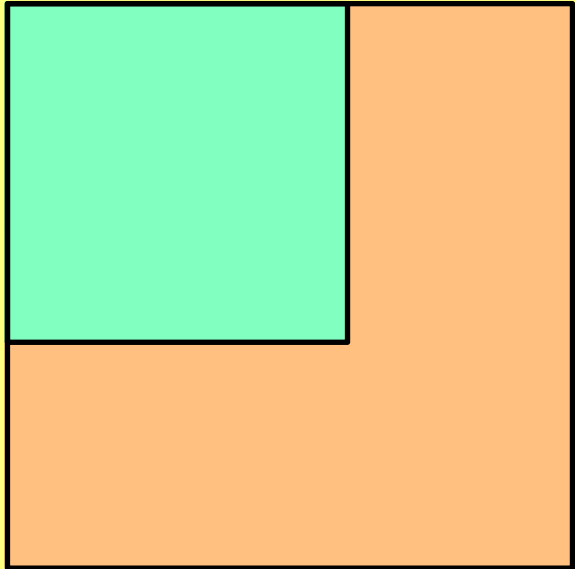
$S_3$  on top



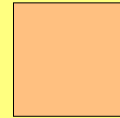
$S_5$  below

$S_5 - S_3$   
=

# Picture Puzzles



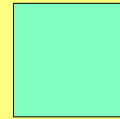
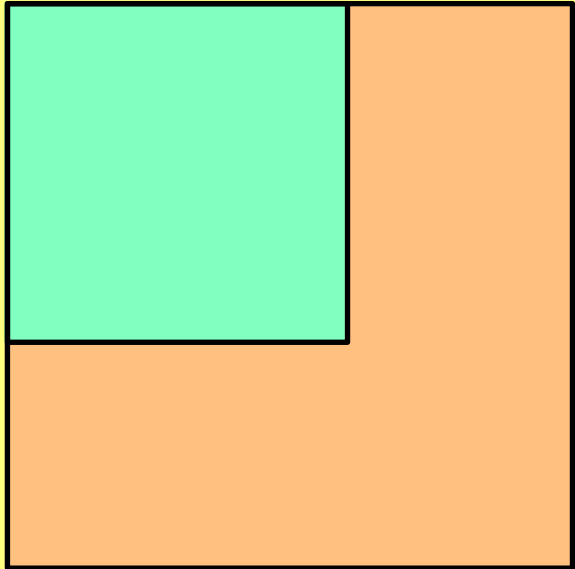
$S_3$  on top



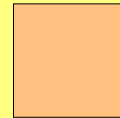
$S_5$  below

$$\begin{aligned} S_5 - S_3 \\ = 25 - 9 \\ = \end{aligned}$$

# Picture Puzzles



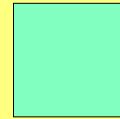
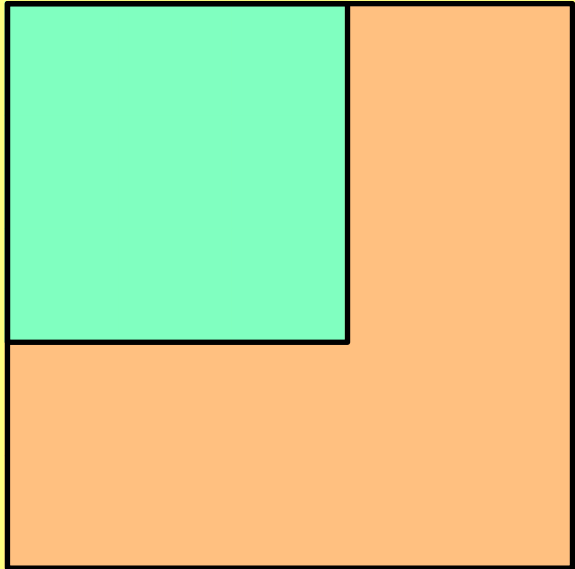
$S_3$  on top



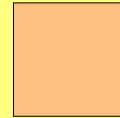
$S_5$  below

$$\begin{aligned} S_5 - S_3 \\ &= 25 - 9 \\ &= 16 \end{aligned}$$

# Picture Puzzles



$S_3$  on top



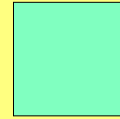
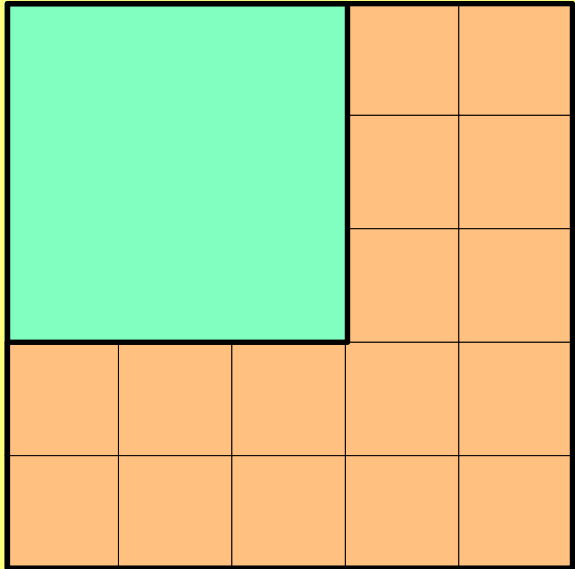
$S_5$  below

$$\begin{aligned} S_5 - S_3 \\ &= 25 - 9 \\ &= 16 \end{aligned}$$

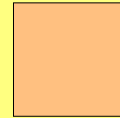
Difference  
between  
two squares



# Picture Puzzles

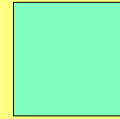
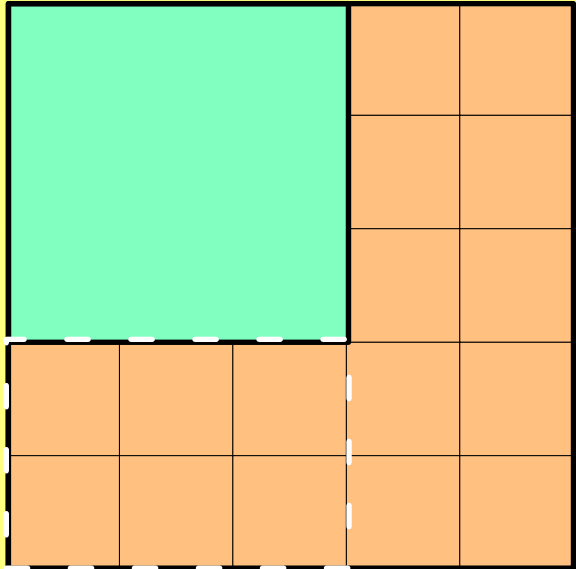


$S_3$  on top

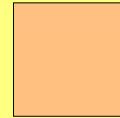


$S_5$  below

# Picture Puzzles

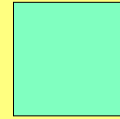
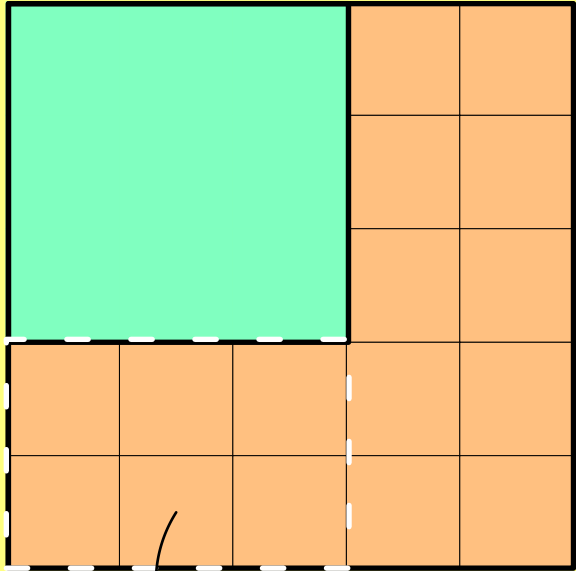


$S_3$  on top

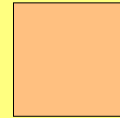


$S_5$  below

# Picture Puzzles

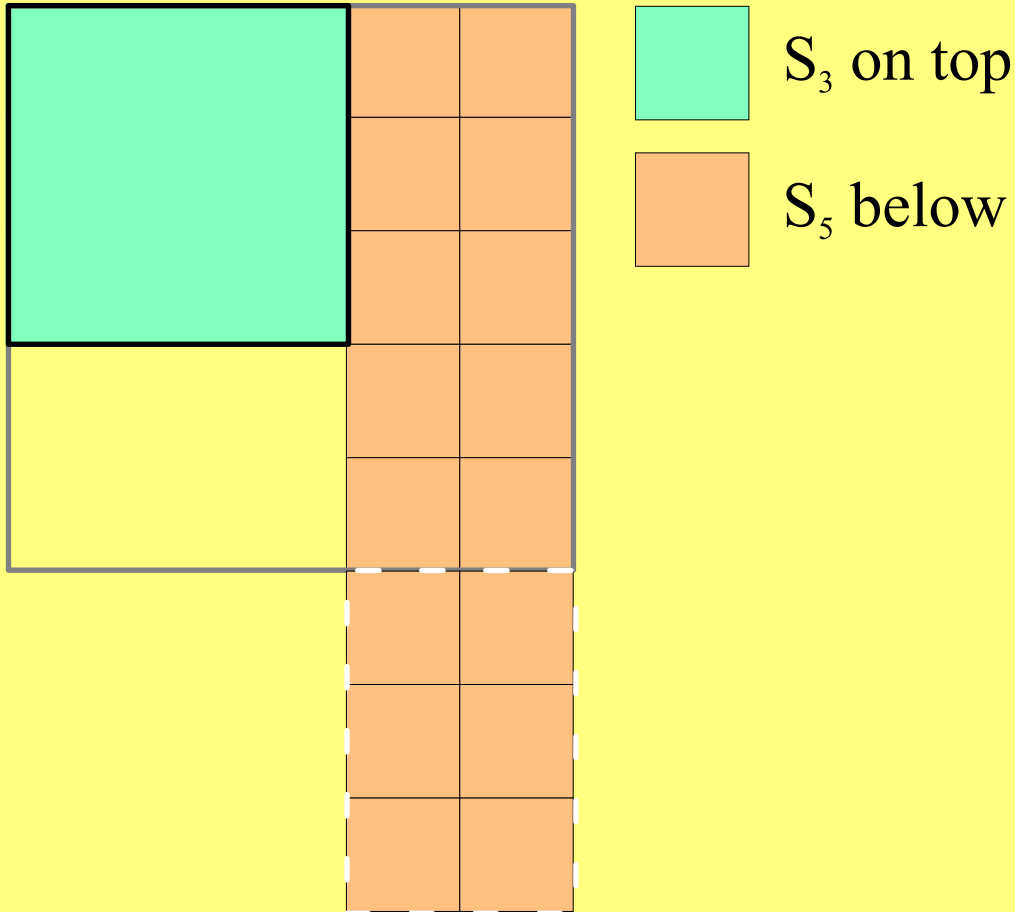


$S_3$  on top

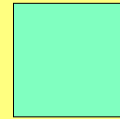
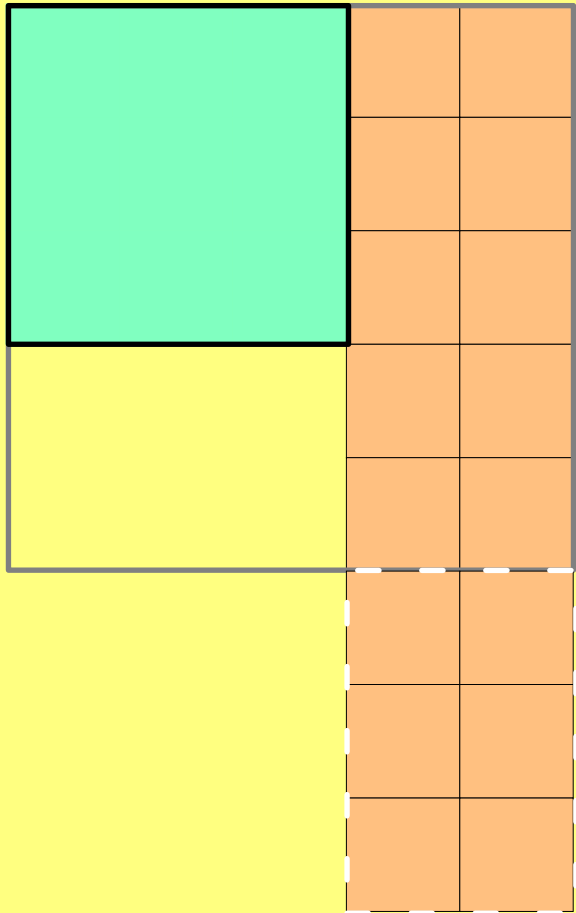


$S_5$  below

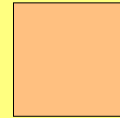
# Picture Puzzles



# Picture Puzzles



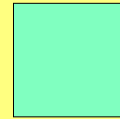
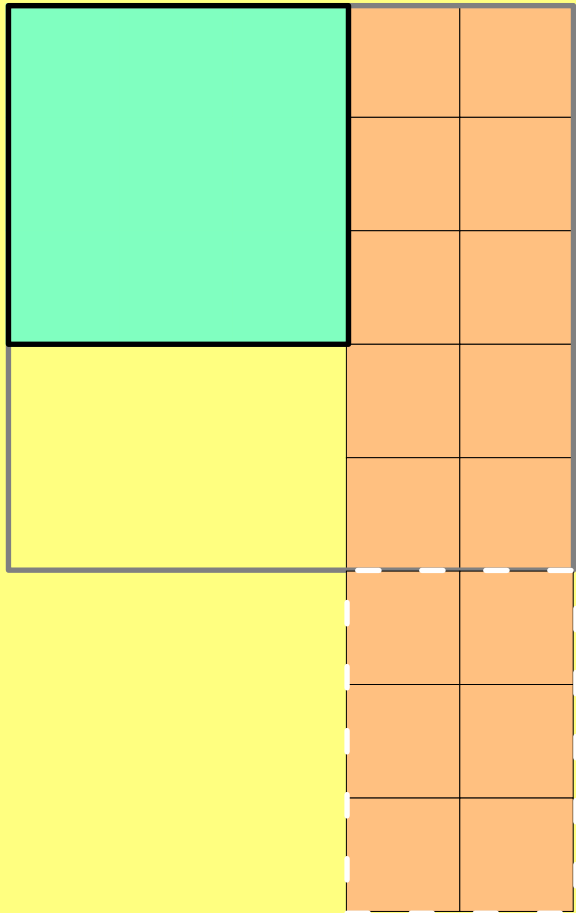
$S_3$  on top



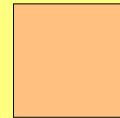
$S_5$  below

$$S_5 - S_3 =$$

# Picture Puzzles



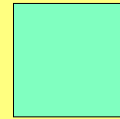
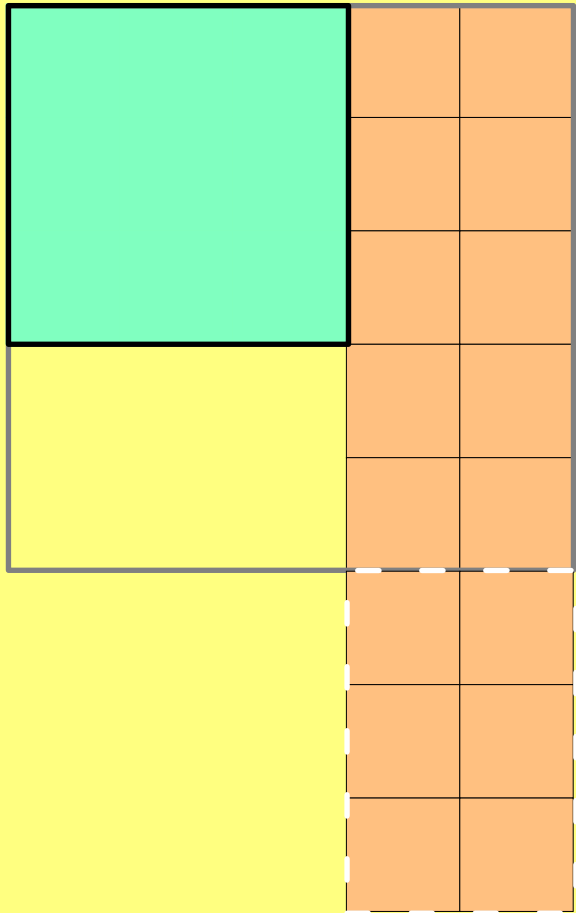
$S_3$  on top



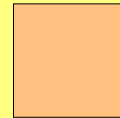
$S_5$  below

$$S_5 - S_3 \\ = (5 + 3) (5 - 3)$$

# Picture Puzzles



$S_3$  on top



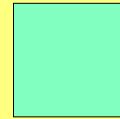
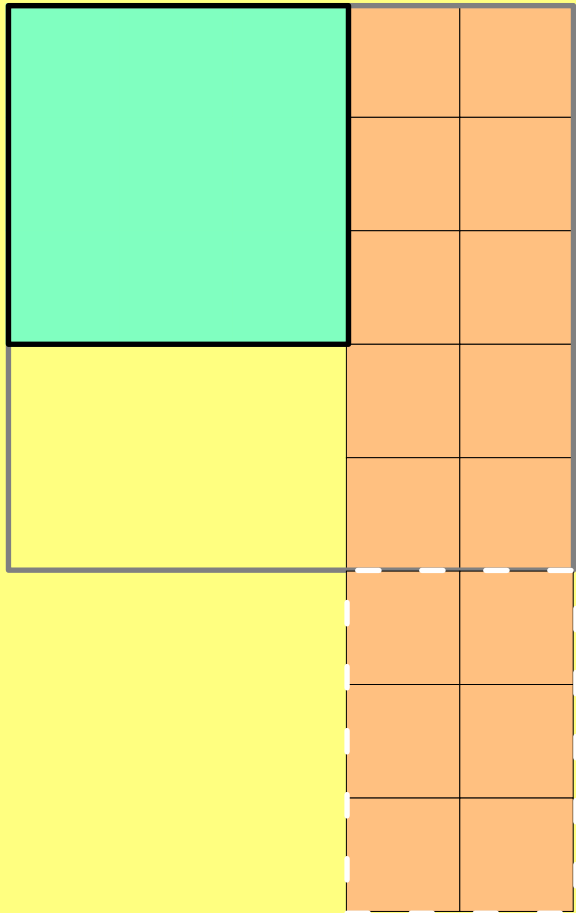
$S_5$  below

$$S_5 - S_3$$

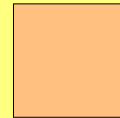
$$= (5 + 3) (5 - 3)$$

Where do these two  
factors come from?

# Picture Puzzles



$S_3$  on top

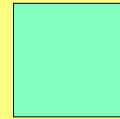
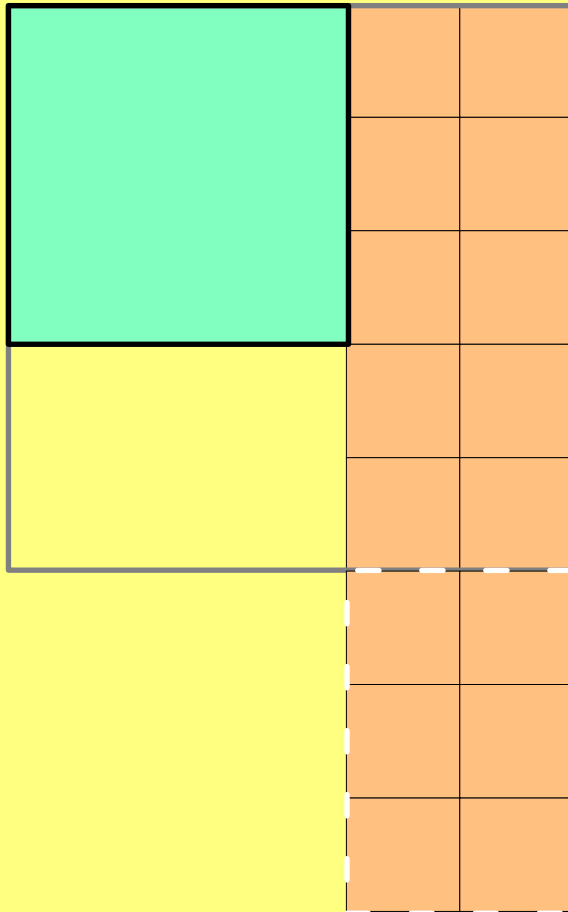


$S_5$  below

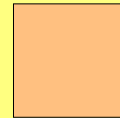
$$\begin{aligned} & S_5 - S_3 \\ &= (5 + 3) (5 - 3) \\ &= 8 \times 2 \\ &= 16 \end{aligned}$$



# Picture Puzzles



$S_3$  on top



$S_5$  below

$$\begin{aligned} & S_5 - S_3 \\ &= (5 + 3) (5 - 3) \\ &= 8 \times 2 \\ &= 16 \end{aligned}$$

Difference  
between  
two squares

**Choose two other squares.**

**Find their difference in two ways.**

**If I tell you the size of any two squares,  
Can you tell me their difference in two ways?**

THE END...

...OR IS IT?